

EE 633
Quiz -II

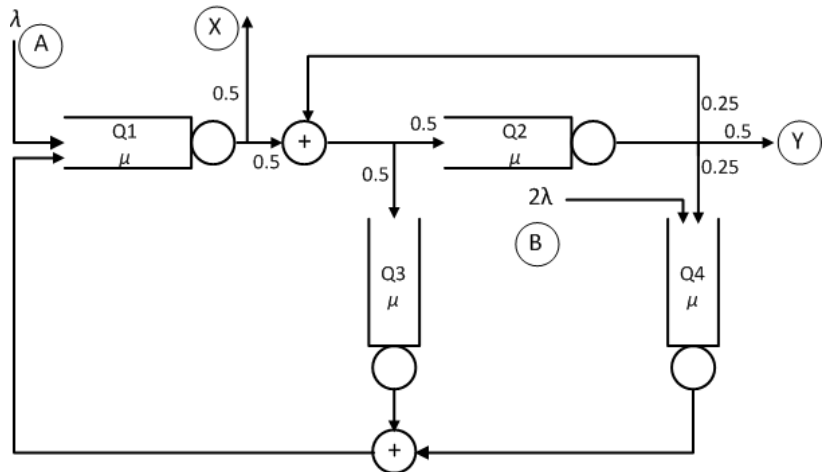
Maximum Marks 10

1. Consider a FCFS $M^{[X]}/G/1$ queue where the arrivals come in batches of one, two or three jobs. The generating function of the batch sizes is given to be $0.25z+0.25z^2+0.5z^3$. The batch arrival rate is λ from a Poisson process.

The first job of the batch has a random service time with its n^{th} moment given as $\alpha(n)$ and the L.T. of its pdf given as $L_\alpha(s)$. The second job of the batch has a random service time with its n^{th} moment given as $\beta(n)$ and the L.T. of its pdf given as $L_\beta(s)$. The third job of the batch has a random service time with its n^{th} moment given as $\gamma(n)$ and the L.T. of its pdf given as $L_\gamma(s)$. The service times of the first, second and third jobs are independent of each other.

What will be the mean queueing delay W_q for an arbitrary job (first, second or third in a batch) and the L.T. $L_{W_q}(s)$ of its pdf? **[5]**

2. Consider the open network of M/M/1 queues as shown where each queue has service rate μ . For notational convenience, use $\rho=\lambda/\mu$



(a) What is the condition for this queueing network to be stable? **[1]**

(b) For $\lambda=0.2$ and $\mu=1$, find the transit delay through the network for each of the following –

(i) Jobs entering from A or B and leaving from X or Y **[2]**

(ii) Jobs entering from A and leaving from X or Y **[2]**